



Overview

University of Sawa
College of Engineering Technology

Air Conditioning and Refrigeration Department

First Stage

Overview

- Coordinates, points, vectors
- Matrices

n D Space

n D Space: \mathbb{R}^n (typically)

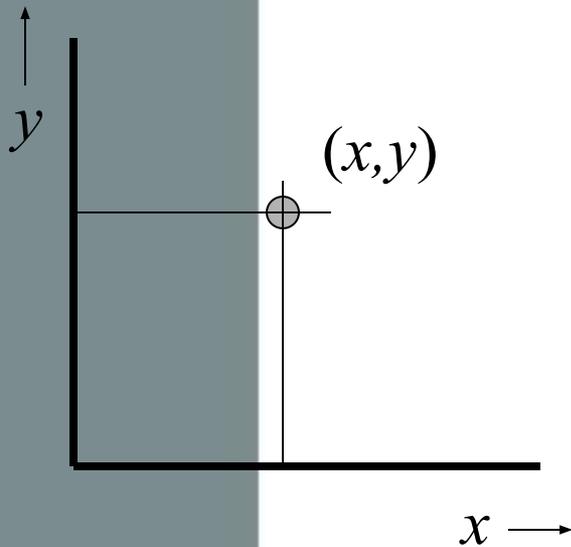
n : number of dimensions

Examples:

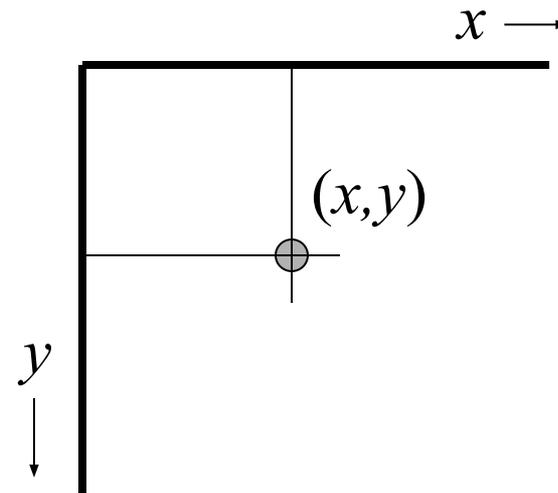
- 1D space: time, along a line or curve
- 2D space: plane, sphere
- 3D space: the world we live in
- 4D space: 3D + time

Coordinates

2D Cartesian coordinates:



Standard



Screen (output, input)

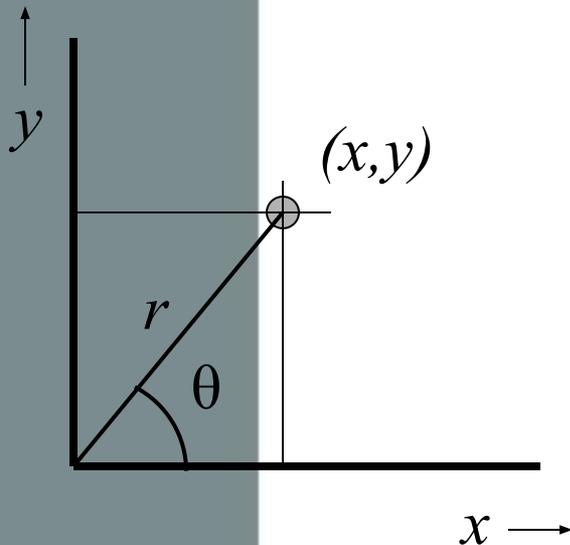
Polar coordinates

Coordinate transformation
from (r, θ) to (x, y) space :

$$x = r \cos \theta$$

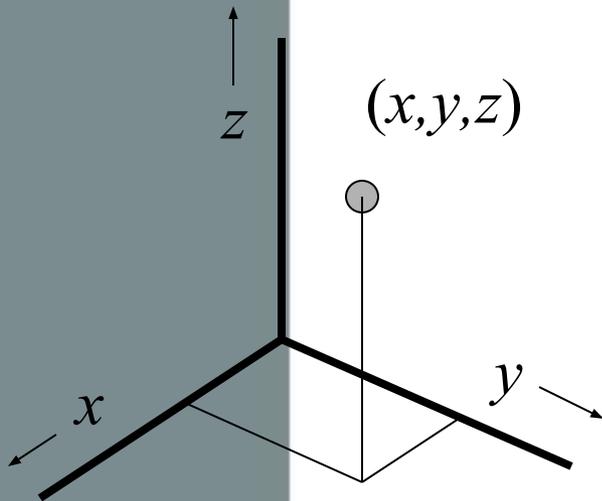
$$y = r \sin \theta$$

Angle θ : in radians

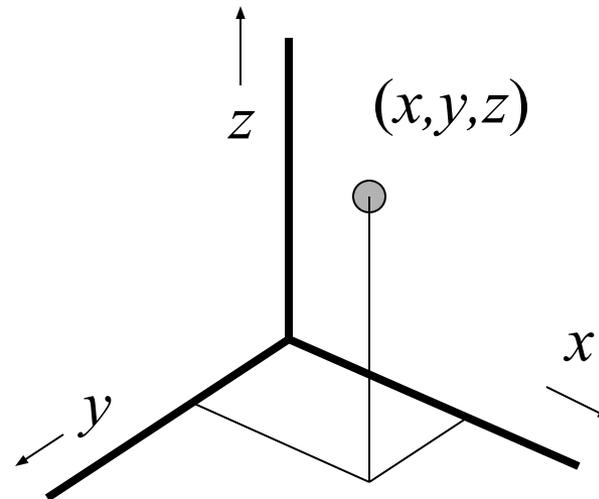


3D coordinates 1

3D Cartesian coordinates:



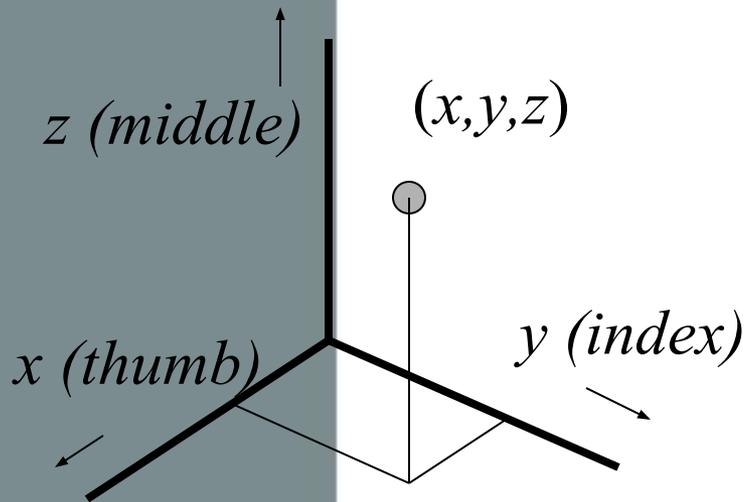
Right-handed



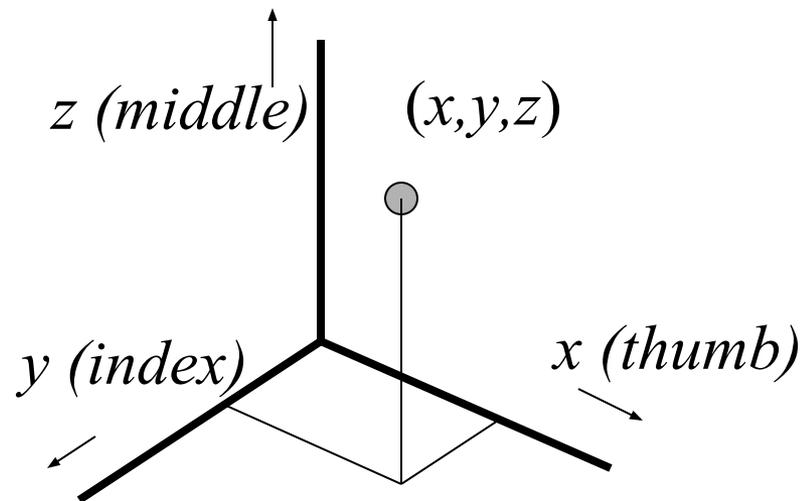
Left-handed

3D coordinates 2

3D Cartesian coordinates:



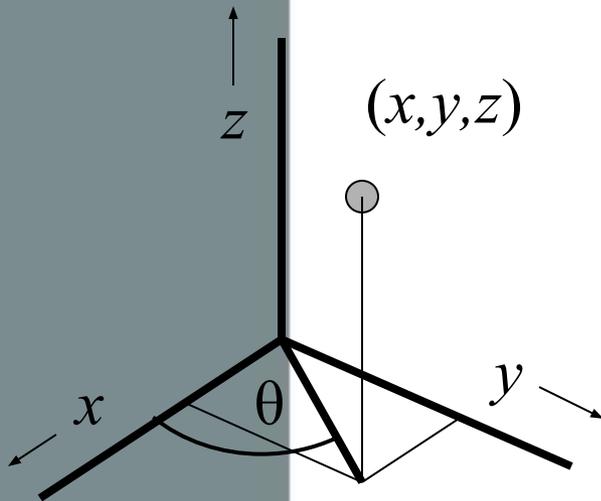
Right-handed



Left-handed

3D coordinates 3

Cylinder coordinates:



$$x = r \cos \theta$$

$$y = r \sin \theta$$

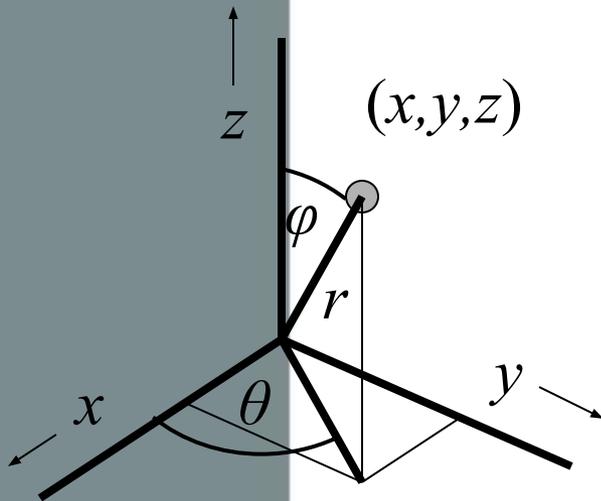
$$z = z$$

3D coordinates 4

Spherical coordinates: $x = r \cos \theta \sin \phi$

$$y = r \sin \theta \sin \phi$$

$$z = r \cos \phi$$



θ : azimuth or longitude

ϕ : elevation or latitude

Also : $\lambda = \pi / 2 - \phi$

λ : colatitude

H&B A-1